

occasion to question the accuracy of these data with regard to the slopes of the density *vs.* temperature lines.

The situation here is similar to that which existed in the case of magnesium and which was discussed by the authors previously.⁴ However, in contrast, there was an abundance of experimental density data for liquid magnesium and it was the *very great discrepancies* between values reported by various workers that first attracted our attention. It was possible to *predict* values for the density at the normal boiling point, critical density, and slope of the density *vs.* temperature line or the temperature coefficient of density for magnesium and these predictions were found subsequently to agree rather closely with our experimental results and extrapolations based thereon. Our calculated results for barium and calcium, obtained by methods to be discussed below, are contrasted with the experimental values in Table I. The discrepancy is substantial.

Table I: Data for Barium and Calcium

	Barium	Calcium
Melting point, °K.	1002 ^a	1123 ^b
Reference density at m.p., g./cm. ³	3.320	1.364
-dD/dT × 10 ⁴ g./cm. ³ °K.		
Experimental	2.14	8.87
Calculated:		
Method 1	5.04	2.18
Method 2	5.10	2.20
Method 3	5.64	2.24
Critical density, g./cm. ³		
Method 1	0.722	0.304
Method 2	0.712	0.299
Method 3	0.620	0.292
Estimated critical temp., °K.	4720 ± 10%	4590 ± 10%
Density at normal boiling point, g./cm. ³		
Method 1	2.862	1.224
Method 2	2.857	1.223
Method 3	2.806	1.220
Normal boiling point, °K.	1910 ^c	1765 ^c
Reduced temperature at normal boiling point	0.405	0.384
ΔH _{vap} at normal boiling point, cal./g. atom	36,070 ^c	35,840 ^c

^a D. T. Peterson and J. A. Hinkebein, *J. Phys. Chem.*, **63**, 1360 (1959). ^b O. Kubaschewski and R. Hörnle, *Z. Metallk.*, **42**, 129 (1951). ^c D. R. Stull and G. C. Sinke, "Thermodynamic Properties of the Elements," *Advances in Chemistry Series*, No. 18, American Chemical Society, Washington, D. C., 1956.

It has been shown⁵⁻⁷ that critical temperatures of metals can be estimated to a fair degree of reliability

by application of the *theorem of corresponding states* to entropy of vaporization data. Critical temperatures estimated on this basis show good agreement with those estimated by use of extrapolated liquid and vapor densities and the law of the rectilinear diameters.

The metal selected as a reference for the application of the theorem of corresponding states is mercury, the only metal whose critical constants have been experimentally determined.⁸ The most reliable data for the entropy of vaporization of mercury are those of Busey and Giauque.⁹ The estimated critical temperatures of barium and calcium together with some other pertinent physical properties are shown in Table I.

Treatment of the data reported by Culpin³ yielded the equation

$$D \text{ (g./cm.³)} = 2.360 - 8.87 \times 10^{-4}T \text{ (°K.)} \quad (1)$$

for the density of liquid calcium. The melting point observed by Culpin was 1075°K., which is considerably lower than 1123°K. as reported by Kubaschewski and Hörnle. No subsequent data have been reported. Without introduction of significant error, the reference density of liquid calcium will be taken as 1.364 g./cm.³ at 1123°K.

The data of Addison and Pulham² fit the equation

$$D \text{ (g./cm.³)} = 3.534 - 2.14 \times 10^{-4}T \text{ (°K.)} \quad (2)$$

for the density of liquid barium. Their measurements covered the range 1013–1103°K. and a slight extrapolation yields a reference density of 3.320 g./cm.³ at the melting point (1002°K.).

It is noted that the temperature coefficient for calcium is very steep and indeed extrapolation of the rectilinear diameter indicates that it crosses the temperature axis at 2660°K., which is well below the critical temperature. The slope in the case of barium, on the other hand, is very slight and leads to a very high

- (1) A report of this work will constitute a portion of a dissertation to be submitted by P. J. McGonigal to the Graduate Board of Temple University in partial fulfillment of the requirements for the degree of Doctor of Philosophy.
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- (3) M. F. Culpin, *Proc. Phys. Soc. (London)*, **203**, 1079 (1957).
- (4) P. J. McGonigal, A. D. Kirshenbaum, and A. V. Grosse, *J. Phys. Chem.*, **66**, 737 (1962).
- (5) A. V. Grosse, *J. Inorg. Nucl. Chem.*, **22**, 23 (1961).
- (6) A. V. Grosse, "The Liquid Range of Metals, and Some of their Physical Properties at High Temperatures," Paper No. 2159, A.R.S., Space Flight Report to the Nation, New York: N. Y., October 9–15, 1961.
- (7) A. V. Grosse, "The Liquid Range of Metals and Some of their Physical Properties at High Temperatures," Report of the Research Institute of Temple University, October 19, 1960.
- (8) F. Birch, *Phys. Rev.*, **41**, 641 (1932).
- (9) R. H. Busey and W. F. Giauque, *J. Am. Chem. Soc.*, **75**, 806 (1953).